

Turbulence state modelling using Machine Learning for fusion plasmas, De Vinci Research Center, Paris

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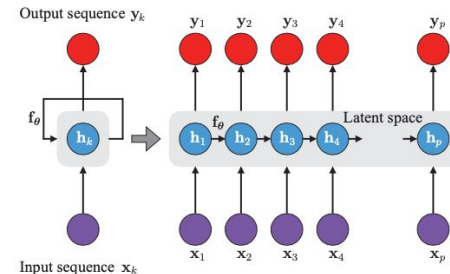
- Like in a predator-prey ecosystem, a system of ODEs can model turbulence and zonal flows occurring in tokamak plasmas [1]
- The system of ODEs is nonlinear and exhibits chaotic behavior
- Neural networks excel at predicting nonlinear patterns from data
- We can use neural networks for **future state predictions** of dynamical systems [2]

$$\frac{dx}{dt} = f(x, \lambda)$$

$$x_{k+1} = x_k + \Delta t f(x_k, \lambda)$$

$$x_{k+1} = x_k + \Delta t g_{\theta}(x_k, \lambda; \theta)$$

- Recurrent Neural Network diagram [2]



[1] Chen, L., Lin, Z., & White, R. (2000). Excitation of zonal flow by drift waves in toroidal plasmas. *Physics of Plasmas*, 7(8)

[2] Brunton, S. L., Kutz, J. N. (2022). *Data-Driven Science and Engineering : Machine Learning, Dynamical Systems, and Control (2nd ed.)*. Cambridge : Cambridge University Press

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Proof of concept

Lotka Volterra system

$$\frac{dx}{dt} = \alpha x - \beta xy$$

$$\frac{dy}{dt} = -\gamma y + \delta xy$$

Recurrent Neural Network and Sliding Window

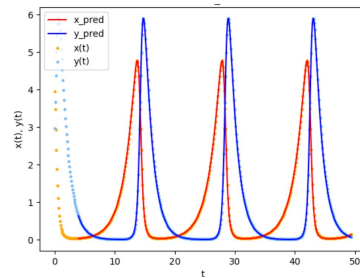
$$g_{\theta} : \mathbb{R}^{7 \times T} \rightarrow \mathbb{R}^2$$

$$\hat{y}_t = g_{\theta}(X_t)$$

$$X_{t+1} = \text{concat}(x_{t-T+2}, x_{t-T+3}, \dots, x_{t+1})$$

$$\hat{y}_{t+1} = g_{\theta}(X_{t+1}), \text{ where } X_{t+1} = [x_{t-T+2}, \dots, x_{t+1}]$$

Example state prediction by Recurrent Neural Network



Data Formatting

RNN input: $\mathbf{X} \in \mathbb{R}^{7 \times T}$: $[x(t), y(t), \alpha, \beta, \gamma, \delta, t]$

RNN output: $[x(t+1), y(t+1)] \in \mathbb{R}^2$