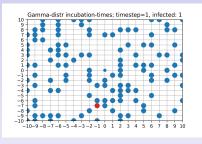
Téo Granger<sup>(a)</sup>, Thomas Michelitsch<sup>(a)</sup>, Bernard Collet<sup>(a)</sup> Michael Bestehorn<sup>(b)</sup>, Alejandro P. Riascos<sup>(c)</sup>



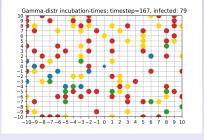


Figure: Colors of indicate health status S  $\subset$  I R of the walkers.

- ullet  $Z\gg 1$  random walkers navigate independently on a  $N\times N$  square-lattice, jumping with probability 1/4 to any of four neighbor lattice points
- Each walker is in one of the states ('compartments')
  - S: susceptible (for infection)
  - C: incubated, infected but not infectious
  - I : infected and infectious
  - R: recovered and immune
- (a) Sorbonne Univ., Institute ∂'Alembert, Campus Jussieu, Paris
- (b) Institute of statistical Physics, Technical Univ. of Cottbus-Senftenberg, Germany
- (c) Institute of Physics, Complex Systems Department, UNAM, Mexico, City , a provide the second second contraction of the second contraction of the

# Four compartment SCIRS model

Infection rule:

If: S meets I on the same lattice point – collision of I and S walkers

Then: the S walker gets infected with probability  $P_{inf}$ 

performing transition

 $S \rightarrow C$  with probability  $P_{inf}$ 

followed by delayed transition  ${\color{black}\mathbb{C}} \to {\color{black}\mathbb{I}} \to {\color{black}\mathbb{R}} \to {\color{black}\mathbb{S}}$ 

with random sojourn times  $t_C$ ,  $t_I$ ,  $t_R$  in the compartments

drawn from probability density functions

$$\mathbb{P}\big(t_{C,I,R} \in [\tau,\tau+\mathrm{d}\tau]\big) = K_{C,I,R}(\tau)\mathrm{d}\tau$$

### Four compartment SCIRS model

Evolution equations s(t) + c(t) + j(t) + r(t) = 1 (constant population without deaths)

$$\frac{d}{dt}s(t) = -\mathcal{A}(t) + (\mathcal{A} \star K_C \star K_I \star K_R)(t)$$

$$\frac{d}{dt}c(t) = \mathcal{A}(t) - (\mathcal{A} \star K_C)(t)$$

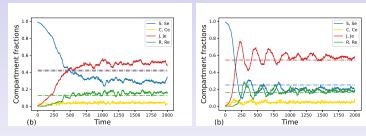
$$\frac{d}{dt}j(t) = (\mathcal{A} \star K_C)(t) - (\mathcal{A} \star K_C \star K_I)(t)$$

$$\frac{d}{dt}r(t) = (\mathcal{A} \star K_C \star K_I)(t) - (\mathcal{A} \star K_C \star K_I \star K_R)(t)$$

 $(a\star b)(t)=\int_0^t a(\tau)b(t-\tau)\mathrm{d}\tau$  stands for convolution  $\mathcal{A}(t)$  infection rate, assumption  $\mathcal{A}(t)=\beta j(t)s(t)$  nonlinear function of j(t) and s(t) describing probability of collision of I and S walkers.

## Four compartment SCIRS model with superspreaders (long-range jumpers)

δ-kernels:  $K_{C,I,R}(\tau) = \delta(\tau - t_{C,I,R})$ , i.e. constant  $t_C, t_I, t_R$  for all walkers



**Left plot:** Epidemic evolution without superspreaders, all walkers perform local jumps.

**Right plot:** 30% superspreaders = fraction of walkers performing long-range jumps

Simulation with Z=100 walkers,  $N^2$  lattice points (N=41), density of walkers  $Z/N^2\approx 0.06$ , infection probability  $P_{inf}=0.9$  with  $t_C=10$ ,  $t_R=40$  and large time of illness  $t_I=130$  sojourn times. We count at each time increment the fractions  $s(t)=\frac{Z_s(t)}{Z}, c(t)=\frac{Z_c(t)}{Z}, j(t)=\frac{Z_l(t)}{Z}, r(t)=\frac{Z_R(t)}{Z}$ .

#### SCIRS model

#### References:

- [1] W.O. Kermack, A.G. McKendrick, A contribution to the mathematical theory of epidemics, Proc. Roy. Soc. A 115, 700–721 (1927)
- [2] T. Granger, T.M. Michelitsch, M. Bestehorn, A. P. Riascos, B. A. Collet, *In Press*, Phys. Rev. E, Preprint: arXiv:2210.09912 (2022).
- [3] M. Bestehorn, T. M Michelitsch, B. A. Collet, A. P. Riascos, A. F. Nowakowski, Phys. Rev. E, 105, 024205, (2022).
- For animated simulations and details of the model consult:

