

# Numerical modeling of turbulent convection in an asymmetric rough Rayleigh-Bénard cell

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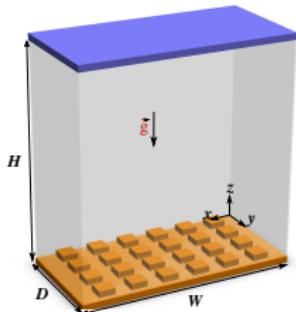


# Asymmetry of temperature field due to roughness

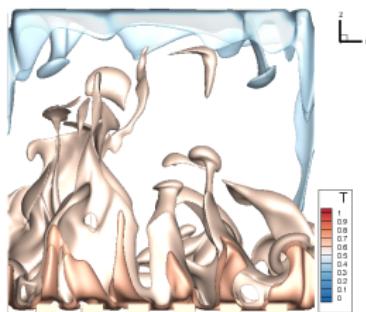
## Rough Rayleigh-Bénard convection: a 5-parameter problem

- 2 physical parameters:  $Ra = \frac{g\beta\Delta TH^3}{\kappa\nu}$ ,  $Pr = \frac{\nu}{\kappa} = 4.38$  (with  $\Delta T = T_{hot} - T_{cold}$ )
- 3 geometrical parameters:  $A_{plot} = H_{plot}/H = 0.03$ ;  $A_W = W/H = 1$ ;  $A_D = D/H = 0.5$

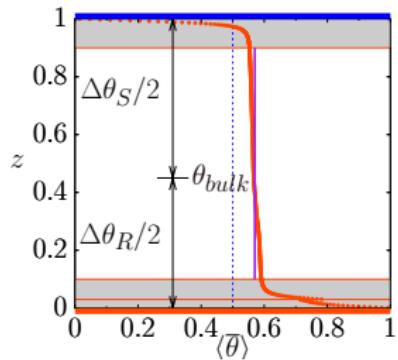
## Geometry and temperature field



Computational domain:  
a Rough/Smooth cavity (*R/S*)



Instantaneous temperature field



Mean vertical profile

Plate separation regarding bulk temperature ( $\theta_{bulk}$ ): two new  $\Delta\theta$  (Tisserand et al. 2011)

- Smooth plate:  $\Delta\theta_S = 2(\theta_{bulk} - \theta_{cold})$

- Rough plate:  $\Delta\theta_R = 2(\theta_{hot} - \theta_{bulk})$

# Intensification of heat transfer ( $Nu$ ) due to roughness

Plate separation regarding bulk temperature ( $\theta_{bulk}$ ): two new  $Ra$ ,  $Nu$  (Tisserand et al. 2011)

- Smooth plate:

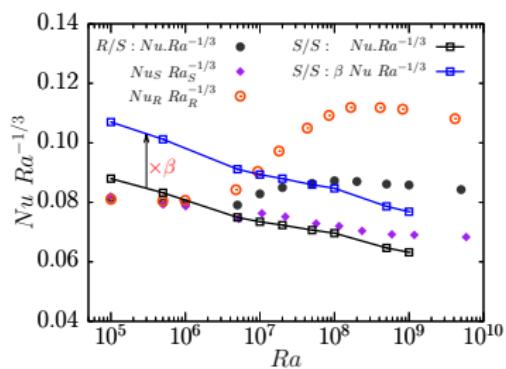
$$\begin{cases} Ra_S = Ra \times (\Delta\theta_S / \Delta\theta) \\ Nu_S = Nu \times (\Delta\theta / \Delta\theta_S) \end{cases}$$

- Rough plate:

$$\begin{cases} Ra_R = Ra \times (\Delta\theta_R / \Delta\theta) \\ Nu_R = Nu \times (\Delta\theta / \Delta\theta_R) \end{cases}$$

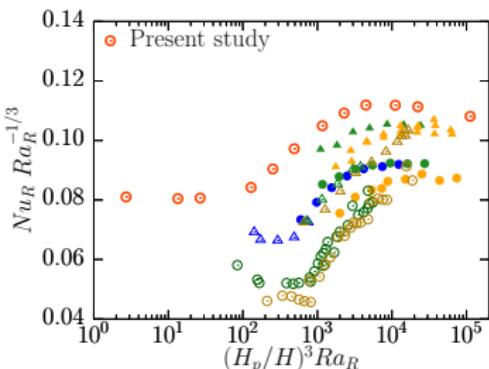
## Compensated Nusselt number ( $Nu$ ) versus Rayleigh number ( $Ra$ )

- Influence of roughness



$$\text{Exchange surface ratio } \beta = \frac{S_R/S}{S_{smooth}}, S \equiv \text{surface}$$

- Good agreement with experimental results



Experimental data from (Rusaouen et al., JFM, 2018)  
 $H_p = 2mm$ : Small cell ( $\triangle$   $\triangle$   $\triangle$ ), Tall cell ( $\circ$   $\circ$ );  
 $H_p = 4mm$ : Small cell ( $\blacktriangle$   $\blacktriangle$ ) and Tall cell ( $\bullet$   $\bullet$   $\bullet$ )